MTH 1125 (2 pm Class) - Test 2

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Name _____

Instructions. Show CLEARLY how you arrive at your answers.

1. Compute:
$$\frac{d}{dx} \left[4x^6 + 6x^4 + 8x^3 + 12x^2 + 24x + \sqrt{x} + 6 \right] =$$

2. Compute:
$$\frac{d}{dx} \left[(8x^2 + 2x) \tan(x) \right] =$$

3. Compute:
$$\frac{d}{dx} \left[\frac{x^4 + x}{\cos(x)} \right] =$$

4. Compute:
$$\frac{d}{dx} \left[\left(4x^5 + 10x^2 + 10x + 10 \right)^{15} \right] =$$

5. Given that $f(x) = 2x^2 - 3x + 2$, give the *equation* of the line tangent to the graph of f(x) at the point (2,4).

6. Given that $x = \sec(t)$ and that $t = 2y^3 + y$; compute $\frac{dx}{dy}$ using the Liebniz form of the Chain Rule. (In particular, when doing this exercise, write the Liebniz form of the chain rule, that you are going to use, explicitly.)

7. Compute:
$$\frac{d}{dx} \left[\sin \left(8x^4 \right) \right] =$$

8. Compute:
$$\frac{d}{dx} \left[\frac{(3x^2+6)^{10}}{(2x^3+6x)^5} \right] =$$

9. Compute:
$$\frac{d}{dx} \left[\sin^3 (8x^2 + 16x) \right] =$$

10. Given that $f(x) = 2x^2 - 5x + 6$, compute f'(x) using the definition of derivative.

11. $x^2 + y^2 = 3x^2y^2$. Compute y'.

Extra (Wow! 10 pts!) Given that $S'(x) = \frac{1}{2S(x)}$ (i.e., $\frac{d}{dx}[S(x)] = \frac{1}{2S(x)}$); compute $\frac{d}{dx}[S(x^2 + x)]$