## Logic Exercise Set \#7-Part 2 Solutions

Spring 2021
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Name $\qquad$

## Instructions

1. Determine the output of the combinatorial circuit:


We follow the processing of the input step by step, yielding:

2. Determine the output of the combinatorial circuit:


We follow the processing of the input step by step, yielding:

3. Find the bitwise OR, bitwise AND, and bitwise XOR of the pair of bit strings: 0101001 and 0100111 0101001 OR $0100111 \equiv 0101111$ (The justification is given below)


0101001 AND $0100111 \equiv 0100001$ (The justification is given below)


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0101001 XOR 0100111 \equiv 0001110 (The justification is given below)
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4. Find the bitwise OR, bitwise AND, and bitwise XOR of the pair of bit strings: 0101001 and 1011000 0101001 OR $1011000 \equiv 1111001$ (The justification is given below)

(1 OR 1)

0101001 AND $1011000 \equiv 0001000$ (The justification is given below)


5. Determine whether the set of System Specifications is consistent:
$\mathrm{s}_{1}$ : The user paid the subscription fee, but does not enter a valid password.
$s_{2}$ : Access is granted if the user has paid the subscription fee and has entered a valid password.
$s_{3}$ : Access is denied if the user has not paid the subscription fee.
$s_{4}$ : If the user has not entered a valid password, but has paid the subscription fee, then access is granted
We represent the simple statements above symbolically, using the following assignments:
p: The user paid the subscription fee
q : The user has entered a valid password
r: Access is granted
Our System specifications are as follows:
$\mathrm{s}_{1}$ : The user paid the subscription fee, but does not enter a valid password. $\quad p \wedge(\neg q)$
$\mathrm{s}_{2}$ : Access is granted if the user has paid the subscription fee and has entered a valid password. $(p \wedge q) \rightarrow r$
$\mathrm{s}_{3}$ : Access is denied if the user has not paid the subscription fee. $\quad(\neg p) \rightarrow(\neg r)$
$\mathrm{s}_{4}$ : If the user has not entered a valid password, but has paid the subscription fee, then access is granted $\quad(\neg q \wedge p) \rightarrow r$

The System Specifications will be consistent exactly when the conjunction of the specifications is NOT a contradiction. (i.e., exactly when the conjunction of the specifications is True for at least one combination of truth values of $\mathrm{p}, \mathrm{q}$, and r .

| $p$ | $q$ | $r$ | $\neg p$ | $\neg q$ | $\neg r$ | $\mathrm{~s}_{1}: p \wedge(\neg q)$ | $(p \wedge q)$ | $\mathrm{s}_{2}:(p \wedge q) \rightarrow r$ | $\mathrm{~s}_{3}:(\neg p) \rightarrow(\neg r)$ | $(\neg q \wedge p)$ | $\mathrm{s}_{4}:(\neg q \wedge p) \rightarrow r$ | $\mathrm{~s}_{1} \wedge \mathrm{~s}_{2} \wedge \mathrm{~s}_{3} \wedge \mathrm{~s}_{4}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| T | T | T | F | F | F | T | T | T | T | F | T | T |
| T | T | F | F | F | T | T | T | F | T | F | T | F |
| T | F | T | F | T | F | T | F | T | T | T | T | T |
| T | F | F | F | T | T | T | F | T | T | T | F | F |
| F | T | T | T | F | F | F | F | T | F | F | T | F |
| F | T | F | T | F | T | F | F | T | T | F | T | F |
| F | F | T | T | T | F | T | F | T | F | F | T | F |
| F | F | F | T | T | T | T | F | T | T | F | T | T |

The fact that "T" appears in the right most column, prevents the conjunction of the system specifications from being a contradiction.

The set of system specifications IS consistent.

