

MTH 4441 Test #1
FALL 2022

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Name _____

1. Define: Group

2. Define: Binary operation

3. Define: Integers a and b **congruent modulo** n .

4. Give an alternate characterization of **congruence modulo** n .

5. Define: (\mathbb{Z}_n, \oplus) (the **additive group of integers modulo** n)

6. Define: (U_n, \odot) (the **multiplicative group of integers modulo** n)

7. Prove: If $(G, *)$ is a group, and a, b are any elements of G , then $(a * b)^{-1} = b^{-1} * a^{-1}$

8. **Define:** The **order of an element** x of a group $(G, *)$ (specify either **additive** or **multiplicative** notation.)

9. **Prove:** The identity element e in a group $(G, *)$ is unique.

10. Construct the group table for (U_5, \odot)

11. In the previous exercise, determine the order of the element 3

12. Construct the group table for (\mathbb{Z}_6, \oplus)

13. In the previous exercise, determine the order of the element 4

14. Determine whether the operation $*$, given by $a * b = ab^2$ is an associative binary operation on the set \mathbb{R} .

15. Fill out the group table below:

$*$	e	a	b	c
e				
a				
b				
c				